

Dynamic Control of Mobile Robot Using RBF Global Fast Sliding mode

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ABSTRACT

This paper mainly in this paper a dynamic control of mobile robot using RBF global fast sliding mode (RBF-GFSM) strategy is presented. Firstly, a GFSM controller is used in order to make the linear and angular velocities converge to references ones in finite time. However, a problem of instability of velocities is appeared by introducing disturbances in the system. Secondly, a combined controller using RBF-GFSM approach is applied in aim to stabilize the velocities errors and estimates the nonlinear function of the robot model. The system stability is done using the Lyapunov theory. The proposed controllers are dynamically simulated using Matlab/Simulink and the simulation results show the efficiency and robustness of the proposed control strategy.

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1. INTRODUCTION

Mobile robots study has attracted important advantage in the robotics and control research community, due to the nonholonomic properties caused by not integrable differential constraints. The mobile robot problem is the motion under nonholonomic constraints using the kinematic model and specially the problem of integration of the nonholonomic kinematic controller with the dynamics of the mobile robot [1]. Mobile robot navigation can be classified into three basic problems [2]; reference trajectory tracking, path following, and situation stabilization. Some nonlinear feedback controllers have been proposed for solving these problems [2]-[4]. The main idea behind these algorithms is to find suitable velocity control inputs which stabilize the closed-loop system.

In recent years, different control techniques have been introduced to control mobile robot. Due to the intrinsic nonlinearity in the mobile robot dynamics and the nonholonomic constraints, nonlinear architectures as adaptive and intelligent methods [5]-[7], backstepping [8], [9] feedback linearization [10] and sliding mode control [11] have been studied. The neural network controller can deal with no modeled bounded disturbances and/or unstructured no modeled dynamics of the mobile robot. Therefore, a control structure that makes possible the integration of a kinematic controller and a neural network (NN) computed-torque controller for nonholonomic mobile robots is presented in [12]. A neuro-fuzzy network (NFN) dynamic controller for mobile robots is presented in [13], with a combined kinematic/dynamic control law is developed using backstepping and stability is guaranteed by Lyapunov theory.

An adaptive neural conventional sliding mode controller for nonholonomic wheeled mobile robots with model uncertainties and external disturbances is presented in [14]. In this work the kinematic model is presented by the polar coordinates and dynamic model with uncertainties is considered. Self recurrent wavelet neural networks (SRWNNs) are used for approximating the model uncertainties and deal

disturbances. In new researches of tracking control, a finite time tracking control was deployed in last year's [15]. A global finite-time tracking controller was given for the nonholonomic systems in [16]. The finite-time tracking control is presented in [17], [18].

For the differential equation of time analysis, the literature proposed finite time stability. So, to study a class of the system stability for a limited time becomes reasonable [19]-[22]. The paper is organized as follows. Section II presents the mobile robot dynamic modeling. Section III resumes RBF neural network. The RBF-GFSM controller is presented in section IV. The simulation and analysis of the improved algorithm are presented in Section V. Finally, conclusions are drawn in Section VI.

2. MOBILE ROBOT MODELING

The mobile robot modeling consists in two models: kinematic and dynamic models. The robot's kinematics is defined by (1):

$$\dot{p} = \begin{pmatrix} \dot{x} \\ \dot{y} \\ \dot{\theta} \end{pmatrix} = \begin{bmatrix} \cos\theta & 0 \\ \sin\theta & 0 \\ 0 & 1 \end{bmatrix} q \quad (1)$$

where q represents the control vector $(v, \omega)^T$.

Generally dynamic modeling is the system motion study in which forces are modeled and it can include energies and the speeds associated with the motions. The general dynamic model of mobile robot can be described by the following equation (2):

$$M(q)\ddot{q} + V(q, \dot{q})\dot{q} + F(\dot{q}) + G(q) + \tau_d = B(q)\tau - A^T(q)\lambda \quad (2)$$

where $M(q)$ is the symmetric positive definite inertia matrix, $V(q, \dot{q})$ is the centripetal and coriolis matrix, $F(\dot{q})$ is the surface friction matrix, $G(q)$ is the gravitational vector, τ_d denoted bounded unknown disturbances including unstructured not modeled dynamics, $B(q)$ is the input transformation matrix, τ is the input vector, $A^T(q)$ is the matrix associated with the constraints, λ is the constraint forces vector. The above system can be transformed into a more suitable representation for control and simulation purposes. The two following matrices are defined to do this transformation as shown in (3-4):

$$\mathcal{G} = \begin{bmatrix} v \\ \omega \end{bmatrix} \quad (3)$$

$$S(q) = \begin{bmatrix} \cos\theta & 0 \\ \sin\theta & 0 \\ 0 & 1 \end{bmatrix} \quad (4)$$

The matrix $S(q)$ has the following relation with matrix $A(q)$ (5):

$$S^T(q)A^T(q) = 0 \quad (5)$$

The equation (2) can be rewritten as shown in (6-10):

$$Mh(q)\dot{\mathcal{G}} + Vh(q, \dot{\mathcal{G}})\mathcal{G} + \tau_h = Bh(q)\tau \quad (6)$$

with:

$$Mh(q) = S^T(q)M(q)S(q) \quad (7)$$

$$\tau_h = S^T(q)\tau_d \quad (8)$$

$$Bh(q) = S^T(q)B(q) \quad (9)$$

$$Vh = S^T(q)M(q)\dot{S}(q) + S^T(q)V^T(q,\dot{q})S \quad (10)$$

Equation (6) is the equation which is used for the control and simulation analysis of the robot. The dynamic modeling of the robot is presented in [23].

3. RBF NEURAL NETWORK

RBF networks are adaptively used to approximate the uncertain nonlinear function. The algorithm of a radial basis function (RBF) networks is defined in [24] as shown in (11):

$$h_j = g(x - c_{ij}^2) / b_j^2 \quad (11)$$

$$f = W^t h(x) + \varepsilon$$

where x is the input state of the network, i is the input number of the network, j is the number of hidden layer nodes. In the network, $h = [h_1 \ h_2 \ \dots \ h_n]^T$ is the output of Gaussian function. W is the neural network weights, and the propagation error is $\varepsilon \leq \varepsilon_N$. RBF network approximation f is used. In Figure 1 is represents an RBF network. The output of RBF network is (12):

$$\hat{f}(x) = \hat{W}^T h(x) \quad (12)$$

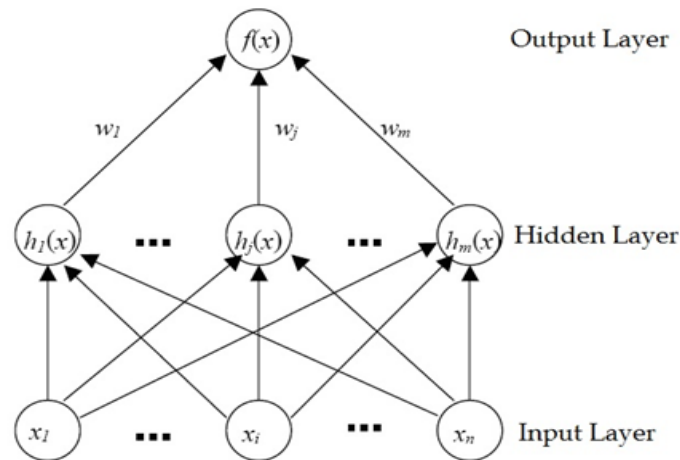


Figure 1. RBF neural network.

The Gaussian function can define as shown in (13):

$$h(x) = \exp\left(-\frac{r^2}{2\sigma^2}\right) \quad (13)$$

4. RBF-GFSM-CONTROLLER

In this work two cases of control are proposed, the first without disturbances, the second in the presence of disturbances. In Figure 2 below resumes the control strategy proposed in this work. The figure below resumes the control strategy proposed in this work.

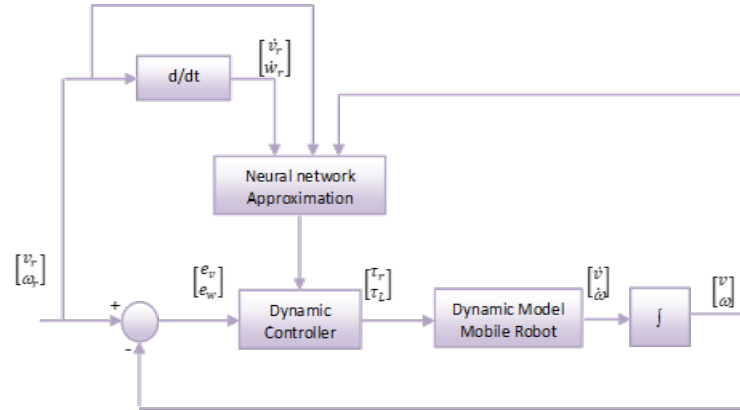


Figure 2. Control strategy

4.1. Control without disturbances

In the case of disturbances absence, the equation (6) becomes (14):

$$Mh(q)\dot{\mathcal{G}} + Vh(q, \dot{q})\mathcal{G} = Bh(q)\tau \tag{14}$$

The velocities errors are definite as shown in (15):

$$e_g = \mathcal{G}_r - \mathcal{G} = \begin{bmatrix} e_v \\ e_w \end{bmatrix} = \begin{bmatrix} v_r - v \\ \omega_r - \omega \end{bmatrix} \tag{15}$$

The derivative of (15) is obtained as shown in (16):

$$\dot{e}_g = \dot{\mathcal{G}}_r - \dot{\mathcal{G}} \tag{16}$$

According to the equation (16), the equation (14) can be rewritten as shown in (17):

$$\begin{aligned} Mh(q)(\dot{\mathcal{G}}_r - \dot{e}_g) + Vh(q, \dot{q})(\mathcal{G}_r - e_g) &= Bh(q)\tau \\ Mh(q)\dot{\mathcal{G}}_r - Mh(q)\dot{e}_g + Vh(q, \dot{q})\mathcal{G}_r - Vh(q, \dot{q})e_g &= Bh(q)\tau \end{aligned} \tag{17}$$

Putting (18):

$$f(x) = Mh(q)\dot{\mathcal{G}}_r + Vh(q, \dot{q})\mathcal{G}_r \tag{18}$$

with $x = [\mathcal{G}_r^T \ \dot{\mathcal{G}}_r^T \ \mathcal{G}^T]^T$

Replacing (18) in (17) and as shown in (19):

$$-Mh(q)\dot{e}_g - Vh(q, \dot{q})e_g + f(x) = Bh(q)\tau \tag{19}$$

The sliding mode controller proposed in this work is based on global fast sliding mode control, this control can make the system states converge to zero in a finite time. A kind of fast terminal sliding surface is proposed as shown in (20):

$$s = \dot{x} + \alpha x + \beta x^{q/p} = 0 \tag{20}$$

Where $x \in R$ is the state and $\alpha > 0$.

The reaching time of the sliding surface to zero is defined as shown in (21):

$$t_s = \frac{p}{\alpha(p-q)} \ln \frac{\alpha x(0)^{\frac{p-q}{p}} + \beta}{\beta} \quad (21)$$

The global fast sliding surface is selected as shown in (22):

$$s = \dot{s}_0 + \alpha s_0 + \beta s_0^{q/p} \quad (22)$$

Where $\beta > 0$ and q, p ($q < p$) are positives odd numbers.

Then, to obtain the control law, a sliding surface is choosing (23):

$$s = e_g \quad (23)$$

$$\text{with: } s = \begin{bmatrix} s_1 \\ s_2 \end{bmatrix}$$

According to the equations (23) and (22), one can have (24):

$$\dot{e}_g = -(\alpha + 1)e_g - \beta e_g^{q/p} \quad (24)$$

Replacing (24) in (19) and as shown in (25):

$$Mh(q) \left((\alpha + 1)e_g + \beta e_g^{q/p} \right) - Vh(q, \dot{q})e_g + f(x) = Bh(q)\tau \quad (25)$$

The control law is obtained as shown in (26):

$$\tau = Bh^{-1}(C_v e_g + f(x) + \beta Mh(q)e_g^{q/p}) \quad (26)$$

Such that (27):

$$C_v = Mh(q)(\alpha + 1) - Vh(q, \dot{q}) \quad (27)$$

4.2. Control in presence of disturbances

In this case, the disturbances are considered; therefore the neural network controller is introduced. The equation (19) is defined as shown in (28):

$$-Mh(q)\dot{e}_g - Vh(q, \dot{q})e_g + f(x) - \tau_d = Bh(q)\tau \quad (28)$$

The control law designed in equation (26) can be rewritten as shown in (29):

$$\tau = Bh^{-1}(C_v e_g + \hat{f}(x) + \beta Mh(q)e_g^{q/p}) \quad (29)$$

when $\hat{f}(x)$ is the output of RBF network. $\hat{f}(x)$ approximates $f(x)$

RBF network can be adopted to approximate $f(x)$. The desired algorithm of RBF network is (30-32):

$$\varphi_i = g(x - c_i^2) / b_i^2 \quad i=1,2,\dots,n \quad (30)$$

$$y = W^{*T} \varphi(x) \quad (31)$$

$$f(x) = W^{*T} \varphi(x) + \varepsilon \quad (32)$$

x is the input state of network, $\varphi(x) = [\varphi_1 \varphi_2 \dots \varphi_n]^T$, ε is the approximation error of network. W^* is the weight vector of desired RBF network. Replacing (29) in (28) and as shown in (33):

$$Mh(q)\dot{e}_g = -(Vh(q, \dot{q}) + C_v)e_g - \beta_3 Mh(q)e_g^{q/p} + \mu_0 \quad (33)$$

when: $\mu_0 = \tilde{f}(x) - \tau_d$, and $\tilde{f}(x) = f(x) - \hat{f}(x)$

The output of the network is giving as shown in (34):

$$f(x) = \hat{W}^T \varphi(x) \quad (34)$$

Selecting: $\hat{W} = W^* - \tilde{W}$, $\|\tilde{W}^*\| \leq W_{\max}$

Therefore (35):

$$\mu_0 = \tilde{f}(x) - \tau_d = \hat{W}^T \varphi(x) + \varepsilon - \tau_d \quad (35)$$

The control law designed in equation (29) can rewrite as shown in (36):

$$\tau = Bh^{-1}\tau = Bh^{-1}(C_v e_g + \hat{f}(x) + \beta Mh(q)e_g^{q/p}) - \xi \quad (36)$$

where ξ is the robust element introduced to eliminate the network approximation error ε and the disturbances τ_d . Replacing the equation (35) in (33) and shown in (37):

$$Mh(q)\dot{e}_g = -(Vh(q, \dot{q}) + C_v)e_g - \beta Mh(q)e_g^{q/p} + \hat{W}^T \varphi(x) + \varepsilon - \tau_d + \xi \quad (37)$$

Putting (38):

$$\mu_1 = \hat{W}^T \varphi(x) + \varepsilon - \tau_d + \xi \quad (38)$$

Replacing (36) in (35) and as shown in (39):

$$Mh(q)\dot{e}_g = -(Vh(q, \dot{q}) + C_v)e_g - \beta Mh(q)e_g^{q/p} + \mu_1 \quad (39)$$

with: $Vh(q, \dot{q}) + C_v = Mh(q)(\alpha + 1)$

The robust element ξ is designed as shown in (40):

$$\xi = -(\varepsilon_N + b_d) \text{sign}(e_g) \quad (40)$$

Where: $\|\varepsilon\| \leq \varepsilon_N$, $\|\tau_d\| \leq b_d$

The candidate function of lyapunov is selected as shown in (41):

$$\rho = \frac{1}{2} e_g^T Mh(q) e_g + \frac{1}{2} \text{tr}(\tilde{W}^T F_w^{-1} \tilde{W}) \quad (41)$$

The derivative of the lyapunov function is defined as shown in (42):

$$\dot{\rho} = e_g^T Mh(q) \dot{e}_g + \frac{1}{2} e_g^T \dot{M}h(q) e_g + \text{tr}(\tilde{W}^T F_w^{-1} \dot{\tilde{W}}) \quad (42)$$

From equation (37) to be (43):

$$\dot{\rho} = -e_g^T Mh(q)(\alpha + 1)e_g - e_g^T \beta Mh(q)e_g^{q/p} + \text{tr}(\tilde{W}^T (F_w^{-1} \dot{\tilde{W}} + \varphi(x)e_g^T)) + e_g^T (\varepsilon - \tau_d + \xi) \quad (43)$$

Select: $\tilde{W} = F_w \varphi(x) e_g^T$

The adaptive rule of network is (44):

$$\hat{W} = F_w \varphi(x) e_g^T \quad (44)$$

Therefore (45):

$$\dot{\rho} = -e_g^T Mh(q)(\alpha+1)e_g - e_g^T \beta Mh(q)e_g^{q/p} + e_g^T (\varepsilon - \tau_d + \xi) \quad (45)$$

Considering the term (46):

$$e_g^T (\varepsilon - \tau_d + \xi) = e_g^T (\varepsilon - \tau_d) + e_g^T \xi = e_g^T (\varepsilon - \tau_d) - \|e_g\| (\varepsilon_N + b_d) \leq 0 \quad (46)$$

Such that matrix Mh define positive, α and β are positives, p and q are positives odd integers ($0 < q/p < 1$); therefore: $\dot{\rho} \leq 0$

5. Simulations and Results

In this section the simulation using Matlab/Simulink is applied on the dynamic mobile robot system. Firstly, the disturbances are excluded, secondly the disturbances are injected, and finally the RBF neural network is introduced to estimate the system nonlinear function and deal the disturbances.

Let us consider: $v_r = 1$ m/s, $\omega_r = 1$ rad/s.

The disturbances $\tau_d = [0.1 \cdot \sin(t) \ 0.1 \cdot \cos(t)]$.

$\alpha=1$, $\beta=2$, $p=7$, $q=5$, $\varepsilon_N=0.2$, $b_d=0.1$.

The neural network is chosen with seven hidden, the initial weight matrix is selected as 0.1. $b=10$. The matrices values of the dynamic model are taken from [25]. Figures 3 and 4 show that actual forward and angular velocities of the control proposed could keep up with the desired ones in absence of disturbances, but the tracking is degraded when the disturbances is appeared, In the case of RBF control the forward and angular velocities could keep up the desired ones in presence of disturbances.

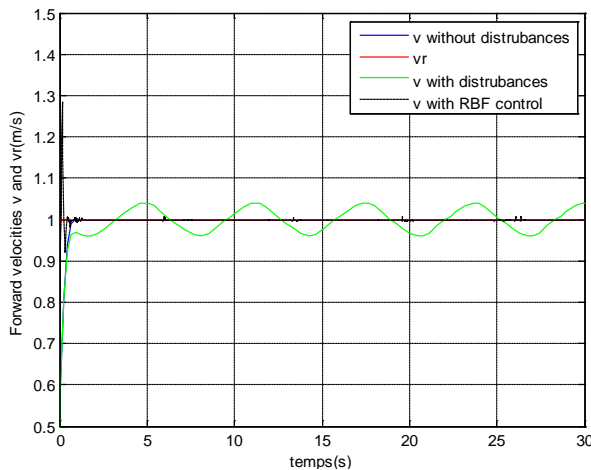


Figure 3. Forward velocities

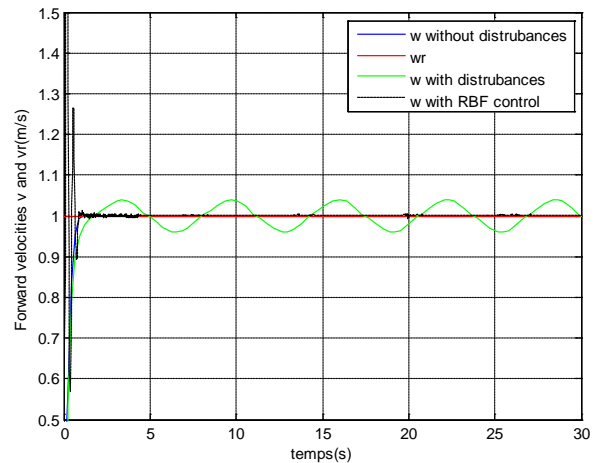


Figure 4. Angular velocities

The figure 5 and 6 show the control torques obtained in presence and absence of disturbances, the torques obtained in the first case are very smooth, when compared with the torques in the second case. In second part of simulations, the sinusoidal reference is considered: $v_r = \cos(2\pi t/5)$, $\omega_r = \sin(2\pi t/5)$. The disturbances $\tau_d = [0.6 \cdot \sin(t) \ 0.6 \cdot \cos(t)]$. In Figure 7 is non-linear and estimate function.

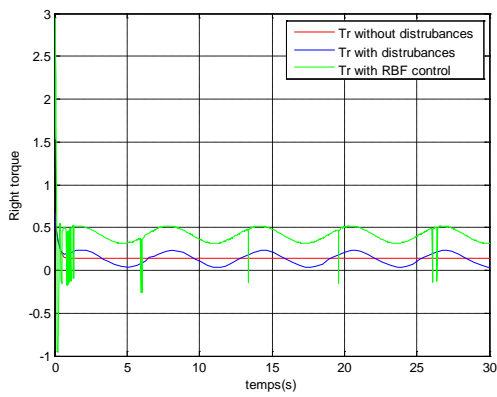


Figure 5. Input right torque

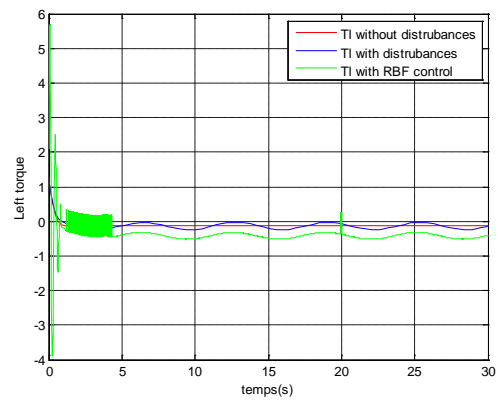


Figure 6. Input left torque

Figures 8 and 9 show that actual linear and angular velocities of the proposed controller could keep up with the desired ones in finite time when the disturbances is excluded, but the tracking is degraded when the disturbances is appeared. In the case of RBF control the linear and angular velocities could keep up the desired ones in presence of disturbances. In Figure 10 is Input right torque. In Figure 11 is input left torque. Figure 12 show the estimated function of the non-linear function.

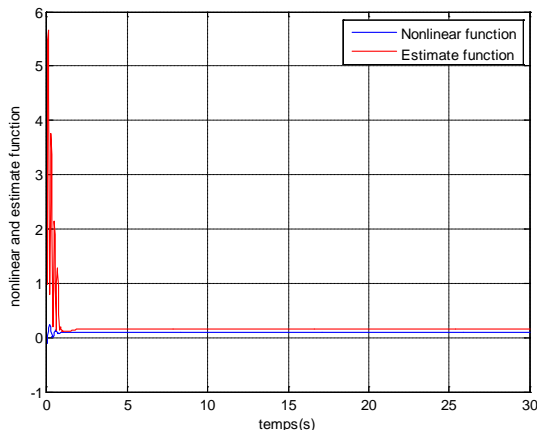


Figure 7. Non-linear and estimate function

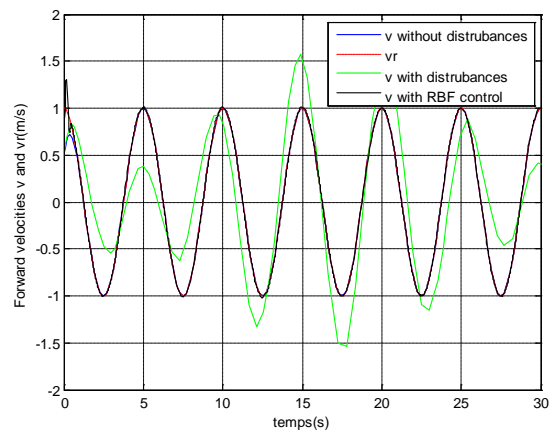


Figure 8. Forward velocities

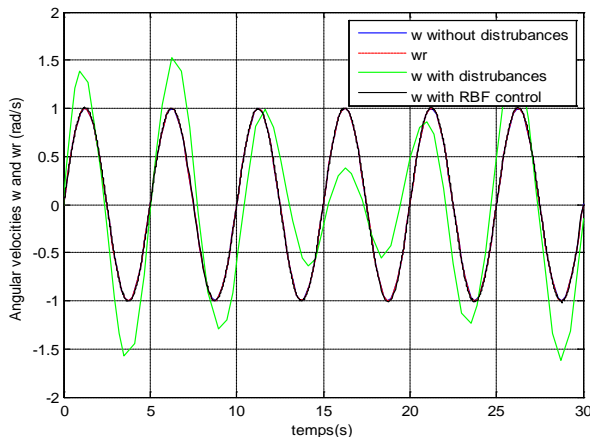


Figure 9. Angular velocities

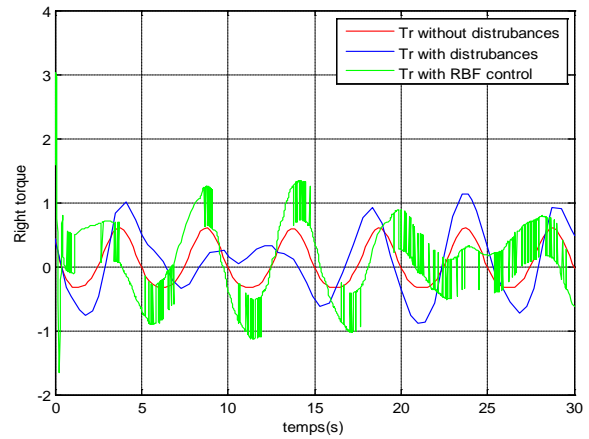


Figure 10. Input right torque

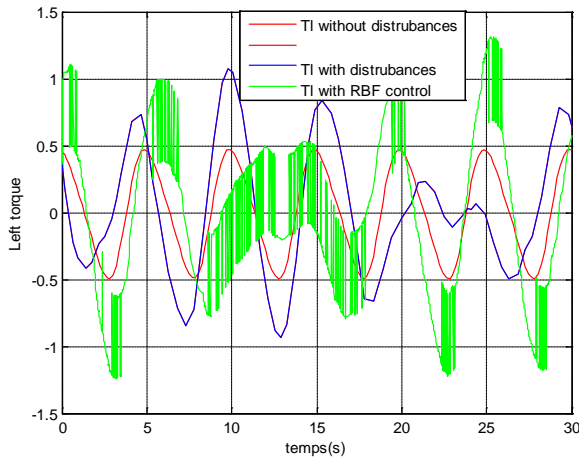


Figure 11. Input left torque

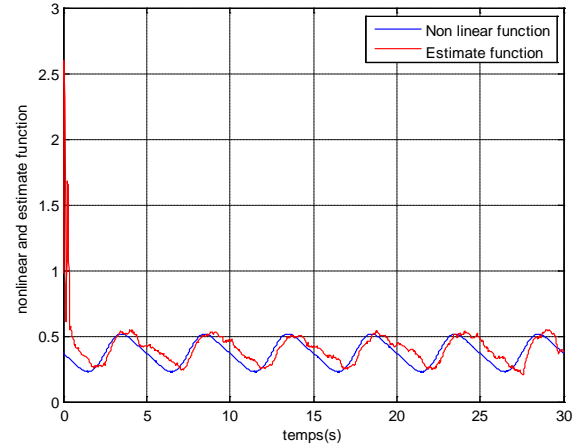


Figure 12. Non-linear and estimate function

6. CONCLUSION

In this paper a RBF-GFSM control is proposed to ensure the dynamic stability of mobile robot. The GFSM control is used in order to make the system converges to the reference in a finite time. The RBF controller stabilizes the velocities errors, deal the disturbances and approximate the system nonlinear function. Simulations results have demonstrated that the RBF-GFSM is efficiency and gives the best performances in comparison with GFSM in the case where the disturbances are introduced.

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