Backstepping Control for MPPT and UPF of a Three Phase Single Stage Grid Connected PV System

M. El malah, A. Ba-razzouk, M. Guisser, E. Abdelmounim, M. Madark
Department of Applied Physics, ASTI Laboratory, FST Settat, Hassan 1st University, Settat, Morocco

ABSTRACT

This paper presents a new control methodology of a three phase grid connected photovoltaic system without using the intermediary DC/DC converter. Based on the synchronized nonlinear model of the whole photovoltaic system, two controllers have been proposed for the three-phase inverter in order to ensure the operation of the PV system at the maximum power point with unity power factor and minimum grid disturbance. Grid synchronization has been ensured by a three-phase 2nd order PLL (Phase-Locked Loop). The stability of each controller is demonstrated by means of Lyapunov analysis and evaluated under changing atmospheric conditions using the Matlab/Simulink environment, the simulation results clearly demonstrate the performance provided by each controller.

Keyword: Backstepping controller
Grid connection
Maximum power point tracking
Unity power factor
PV systems

Copyright © 2018 Institute of Advanced Engineering and Science. All rights reserved.

1. INTRODUCTION

Human demands for energy will not decrease so we are going to run out of fossil fuels for energy. Nuclear energy is not likely to be a major source of world energy consumption because of the relative risks associated with unleashing the power of the atom and we have no choice but to invest heavily in renewable energy production. Solar energy is one of the most promising renewable sources of electricity power in the world. Moreover, the coordinated inter-connection of solar energy sources between global electricity markets can supply more flexibility and balancing to the grid. This is why the grid-connected photovoltaic systems have a great bright future.

Achieving the reduction of PV system manufacturing costs remains a major task. Among the trends to achieve such a reduction is the elimination of the DC/DC converter stage. Conventionally, the first converter stage, which is usually placed between the PV arrays and the inverter [1]-[3], achieves the MPPT whereas the inverter stage delivers and controls the energy injected into the grid. Therefore, to achieve this cost reduction, the three-phase inverter must also take care of the maximum power point tracking.

Maximum power point tracking is mandatory to maximize photovoltaic systems efficiency. To this end, several MPPT control strategies have been largely published in the last few years [1]-[8]. Perturb and observe (P&O) and incremental conductance (IC) algorithms are the most widely proposed in literature. They are the simplest algorithms to implement [3]-[5], but the dilemma -the choice between convergence speed and output fluctuations [5], [6], has led in recent years to several research aimed at improving these two techniques [9], [10]. The nonlinearity of photovoltaic characteristics makes the control of PV systems by conventional control strategies a complex task. However, the recent involvement of nonlinear controls has enriched the field of research and has proved most appropriate for the control of nonlinear systems [7], [8]. In particular, [6] and [11] are comparative studies between the backstepping control and other conventional controls which clearly showed the performance of the backstepping control.

In this paper, two controllers for the three-phase inverter, based on backstepping approach, are proposed and discussed. The first control objective is to track the maximum power point ($\frac{\partial P_p}{\partial V_p}=0$). The second objective is to ensure a grid connection with unity power factor (output current must be in phase with the grid voltage). The proposed controllers are developed in the synchronous orthogonal frame and the voltage phase angle of the grid utility is detected using a three-phase PLL (Phase-Locked Loop).

This paper is organized as follows. In section two, the system description and the mathematical model are presented. Section three develops the control strategies of proposed system. Simulation results are presented and compared in section four. In the last section, a conclusion followed by the reference list.

2. DESCRIPTIONS AND MODELING OF PV SYSTEM

It is essential to find a simple cell model that would be useful for PV application. The PV cell is basically a p-n semiconductor junction that converts light energy into electrical energy. The PV cell can be represented by a current source controlled by voltage, sensitive to temperature and solar radiation, in parallel with one diode and a shunt resistor $R_{sh}$ and the whole is in series with a resistor $R_s$ (Figure 1). The mathematical model of solar cells is detailed in [3]. Although it is a simplified model, this equivalent circuit is sufficiently accurate to represent the different types of photovoltaic cells. According to [12], both resistors ($R_s$ and $R_{sh}$) may be neglected. However, it is demonstrated that the series resistor ($R_s$) has a significant impact on the accuracy, between the maximum power operating point and the open circuit voltage, of the current-voltage characteristic curve inclination.

The photovoltaic array is a multiple associations, in series and parallel, of PV cells. The PV generator considered in this paper is composed by thirty-three SM55 Siemens panels connected in series. The electrical specifications for one panel are enlisted in Table 1. The modeling of the SM55 panel, using Matlab/Simulink, allowed tracing its characteristics for different values of irradiance and temperature which are shown in Figure 2 and Figure 3. Figure 4 shows the power-voltage characteristics of the PV generator considered in this paper under changing climatic conditions. The coordinates of the Maximum Power Points (MPPi) are summarized in Table 2, and will be used for the verification of the simulation results.

Table 1. Electrical Specifications for SM55 Solar Panel

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Maximum power</td>
<td>35W</td>
</tr>
<tr>
<td>Current at the maximum power point</td>
<td>3.15A</td>
</tr>
<tr>
<td>Voltage at the maximum power point</td>
<td>17.4V</td>
</tr>
<tr>
<td>Maximum current (short circuit output)</td>
<td>3.45A</td>
</tr>
<tr>
<td>Maximum voltage (open circuit)</td>
<td>21.7V</td>
</tr>
<tr>
<td>Current temperature coefficient</td>
<td>1.2mA/°C</td>
</tr>
<tr>
<td>Number of series cells $N_s$</td>
<td>36</td>
</tr>
<tr>
<td>Number of parallel modules $N_p$</td>
<td>1</td>
</tr>
</tbody>
</table>

Figure 1. Equivalent circuit of PV cell

Figure 2. Power-voltage characteristics for the SM55 panel at 1000W/m2 with varying temperature levels.

References

[12]
Figure 3. Power-voltage characteristics for the SM55 panel at 25°C with varying radiation levels.

Figure 4. Power-voltage characteristics of the proposed PV-Generator

Table 2. Maximum Power Points (MPP) In Figure 4

<table>
<thead>
<tr>
<th>Maximum power point</th>
<th>Voltage [V]</th>
<th>Power [W]</th>
</tr>
</thead>
<tbody>
<tr>
<td>MPP1</td>
<td>584</td>
<td>1847</td>
</tr>
<tr>
<td>MPP2</td>
<td>531.6</td>
<td>1447.8</td>
</tr>
<tr>
<td>MPP3</td>
<td>573.2</td>
<td>1119</td>
</tr>
</tbody>
</table>

The basic power circuit of proposed single stage PV-system (Figure 5) consists of a DC-link capacitor which is directly connected to the three-phase IGBT inverter. Grid connection was performed through a low-pass filter used to reduce the ripple components due to the switching actions in PWM inverter. It is assumed that all three phase inverter switches are ideal, the low-pass filter phases are identical ($L_1=L_2=L_3=L$ & $R_1=R_2=R_3=R$) and the grid voltage is symmetric. The three-phase model of the inverter with its low-pass filter is detailed in [7]. A simplified model can be obtained in the synchronous orthogonal frame rotating at the angular frequency of the grid voltage. For this purpose, the power-invariant qd-transformation, from balanced three phase electrical quantities to balanced two phase quadrature quantities, has been used. The abc-qd transformation matrix is given below (1):

$$T(\theta) = \sqrt{\frac{2}{3}} \begin{bmatrix} \cos(\theta) & \cos(\theta - \frac{2\pi}{3}) & \cos(\theta + \frac{2\pi}{3}) \\ -\sin(\theta) & -\sin(\theta - \frac{2\pi}{3}) & -\sin(\theta + \frac{2\pi}{3}) \end{bmatrix}$$

where $\theta$ is the angular position of the dq-frame. The state-space model can be re-written in the new reference frame, as (2) [7]:

$$\begin{cases} i_d = \frac{-R}{L}i_d + \omega i_q - \frac{E_d}{L} + \frac{V_p}{L}K_d \\ i_q = -\omega i_d + \frac{R}{L}i_q - \frac{E_q}{L} + \frac{V_p}{L}K_q \\ \dot{V}_p = \frac{1}{C}(I_p - I_dK_d - I_qK_q) \end{cases}$$

where: ($I_p, V_p$): PV array current and voltage; ($K_d, K_q$): Direct and quadrature inverter control inputs; ($I_d, I_q$): Direct and quadrature injected current components; ($E_d, E_q$): Grid direct and quadrature voltages;

$$\begin{bmatrix} K_d \\ K_q \end{bmatrix}^T = T(\theta)[k_1 \ k_2 \ k_3]^T; \quad [I_d \\ I_q]^T = T(\theta)[i_1 \ i_2 \ i_3]^T; \quad [E_d \\ E_q]^T = T(\theta)[e_1 \ e_2 \ e_3]^T$$

3. CONTROLLER DESIGN

In order to match with the proposed modeling presented earlier (2), the three-phase grid currents and voltages are transformed into direct and quadrature axis components. The controller outputs ($K_d$ & $K_q$) are then transformed into three-phase components using the inverse dq-abc transformation, and then a PWM control is used to make them suitable for switching the inverter switches (Figure 6).

The injected currents have to be synchronized with the grid voltages. To this end, the grid voltage phase angle is detected using a 2nd order phase locked loop (PLL). The structure of the PLL implemented in...
this work (Figure 7) uses the grid voltage abc-dq transformation to track the grid voltages phase angle. A PI regulator was used to generate a corrective phase angle \( \theta_{\text{est}} \), that is fed back into the grid voltage abc-dq transformation module, from the quadrature voltage error [13]. The block diagram representation of the backstepping control approach is illustrated in the following Figure.
Finally, when the PV-generator power is at its maximum state, (Figure 3), its derivative with respect to PV-voltage is zero. Table 3 summarizes the selected dynamic outputs and their references for each controller.

Table 3. Dynamic outputs and their references

<table>
<thead>
<tr>
<th>Controller</th>
<th>The dynamic output considered</th>
<th>Output Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>First</td>
<td>$y = \begin{bmatrix} y_1 \ y_2 \end{bmatrix} = \begin{bmatrix} \frac{\partial P_p}{\partial y_p} \ e_d^2 + e_q^2 \end{bmatrix}$</td>
<td>$y_{\text{ref}} = \begin{bmatrix} \frac{\partial P_p}{\partial y_p} \text{ref} \ (e_d^2 + e_q^2)_{\text{ref}} \end{bmatrix} = \begin{bmatrix} 0 \ 0 \end{bmatrix}$</td>
</tr>
<tr>
<td>Second</td>
<td>$y = \begin{bmatrix} y_1 \ y_2 \end{bmatrix} = \begin{bmatrix} \frac{\partial P_p}{\partial y_q} \ \frac{\partial P_p}{\partial y_q} \text{q}_{\text{ref}} \end{bmatrix}$</td>
<td>$y_{\text{ref}} = \begin{bmatrix} \frac{\partial P_p}{\partial y_q} \text{ref} \ I_n_{\text{ref}} \end{bmatrix} = \begin{bmatrix} 0 \ 0 \end{bmatrix}$</td>
</tr>
</tbody>
</table>

where: $e_d = I_d - I_{\text{dref}}$ is the direct current error, $e_q = I_q - I_{\text{qref}}$ is the quadrature current error.

The output chosen for the second controller is simpler than the first, but it is a challenging and time-consuming task to tune the appropriate backstepping parameters in this controller. This is largely due to the fact that establishing stability for switched systems is difficult. Therefore, in the first controller, we have chosen to also involve the direct current component $I_d$ in the control of the output power.

### 2.1. Formulation of MPPT control law (controller 1&2)

Let us define the first tracking error $\epsilon_1$ and its LFC (Lyapunov Function Candidate) $V_1$, using (2), it is possible to deduce (5-6):

$\epsilon_1 = y_1 - y_{1\text{ref}} = I_p + V_p \frac{\partial I_p}{\partial V_p} \Rightarrow \dot{\epsilon}_1 = \left( V_p \frac{\partial I_p}{\partial V_p} \right) \frac{\partial I_p}{\partial V_p} + 2 \frac{\partial I_p}{\partial V_p} \dot{V}_p \equiv f(p - I_d K_d - I_q K_q)$

$V_1 = \frac{1}{2} \epsilon_1^2 \Rightarrow \dot{V}_1 = \epsilon_1 \dot{\epsilon}_1 = \frac{\epsilon_1 f}{C} (p - I_d K_d - I_q K_q)$

where: $f = V_p \frac{\partial I_p}{\partial V_p} + 2 \frac{\partial I_p}{\partial V_p}$. The stabilizing controls $K_d$ and $K_q$ is chosen as follows (7):

$B_1 + A_1 K_d + A_2 K_q = 0$ (7)

where: $B_1 = \frac{I_p f}{C} + c_1 \epsilon_1$, $A_1 = \frac{I_q f}{C}$, $A_2 = \frac{I_q f}{C}$ and $c_1$ is a positive design parameter.

With the above choice $\dot{V}_1 = -c_1 \epsilon_1^2$ becomes defined negative, $\epsilon_1$ is proved to be asymptotically stable and converge to zero by the Lyapunov design. This means that $y_1 \rightarrow y_{1\text{ref}}$, so $P_p \rightarrow (P_p)_{\text{MPP}}$.

### 2.2. Formulation of output power control law

#### 2.2.1. First controller

According to Table 3 we define the error $\epsilon_2$ and its derivative are deduce from (2) will be (8):

$\begin{cases} 
\epsilon_2 = y_2 - y_{2\text{ref}} \\
\dot{\epsilon}_2 = 2 e_d \left( -R I_d + \omega I_q - \frac{e_d}{L} + \frac{V_p}{L} K_d - I_{\text{dref}} \right) + 2 e_q \left( -\omega I_d + \frac{R}{L} I_q + \frac{V_p}{L} K_q \right)
\end{cases}$

Where: $I_{\text{dref}} = \frac{P_p}{e_d} = \frac{\epsilon_1 V_p}{e_d} \left( I_p - I_d K_d - I_q K_q \right)$
Let us consider the following new LFC and its derivative with respect to time deduce from (8) will be (9):

\[
\begin{align*}
V_2 &= V_1 + \frac{1}{2} \varepsilon_2^2 \\
V_2 &= -c_1 \varepsilon_1^2 + 2 \varepsilon_2 e_d (\frac{-R}{L} I_d + \omega I_q - \frac{e_d}{L} + \frac{v_p}{L} K_d - \hat{i}_{dref}) + e_q (\omega I_d + \frac{R}{L} I_q + \frac{v_p}{L} K_q)
\end{align*}
\]

Then the stabilizing controls for the second step ($K_d$ and $K_q$) is chosen as follows (10):

\[
B_2 + A_3 K_d + A_4 K_q = 0
\]

where:

\[
A_3 = e_d \frac{v_p}{L} + \frac{e_s}{L} I_q ; A_4 = e_q \frac{v_p}{L} + \frac{e_s}{L} I_q ; B_2 = \frac{1}{2} c_2 \varepsilon_2 + e_d \left( \frac{-R}{L} I_d + \omega I_q - \frac{e_d}{L} \right) + e_q \left( -\omega I_d - \frac{R}{L} I_q \right)
\]

is a positive parameter. With the above choice $\tilde{V}_2 = -c_1 \varepsilon_1^2 - c_2 \varepsilon_2^2 < 0$, $\varepsilon_1$ and $\varepsilon_2$ are proved to be stable and converge to zero by the Lyapunov design. This means that $y$ converge to $y_{ref}$. We are finally in a position to determine the stabilizing control signals, $K_d$ & $K_q$, from (7) and (10) will be (11):

\[
\begin{bmatrix}
A_1 & A_2 \\
A_3 & A_4
\end{bmatrix}
\begin{bmatrix}
K_d \\
K_q
\end{bmatrix}
= -
\begin{bmatrix}
B_1 \\
B_2
\end{bmatrix}
\]

2.2.2. Second controller

The tracking error $\varepsilon_2$ is reduced to (12):

\[
\varepsilon_2 = I_q - I_{qref} = I_q \quad \text{From (2)} \Rightarrow \dot{\varepsilon}_2 = -\omega I_d + \frac{-R}{L} I_q - \frac{e_d}{L} + \frac{v_p}{L} K_q
\]

And the control low $K_q$ can be extracted directly from the second equation of mathematical model (2), by choosing $K_d$ such that (13):

\[
K_q = \frac{L}{v_p} (-c_2 I_q + \omega I_d + \frac{R}{L} I_q) \Leftrightarrow \dot{\varepsilon}_2 = -c_2 \varepsilon_2 \Rightarrow \tilde{V}_2 = \dot{V}_1 + \varepsilon_2 \dot{\varepsilon}_2 = -c_1 \varepsilon_1^2 - c_2 \varepsilon_2^2
\]

Using (7) and (13) will be (14):

\[
\begin{bmatrix}
K_d \\
K_q
\end{bmatrix}
= -
\begin{bmatrix}
A_1 & A_2 \\
0 & \frac{v_p}{L}
\end{bmatrix}^{-1}
\begin{bmatrix}
B_1 \\
B_2
\end{bmatrix}
\]

4. SIMULATION RESULTS

The theoretical performances of the proposed controllers discussed in section three will be illustrated by simulation in this section. The PV system (Figure 6) is simulated jointly with each controller, using the instantaneous three phase model, in Matlab/Simulink environment (Figure 8). The model in d-q axis (2) is only used in the controllers design. Important simulation parameters are given in the Table 4. Controllers’ parameters have been selected using a ‘trial-and-error’ search method. In order to prove the robustness of the control algorithms, the simulation is performed with the following scenario:

- A temperature increase from $T=25^\circ C$ (298.15K) to $T=45^\circ C$ (318.15K) after 1sec of start of simulation, then returns to $T=25^\circ C$ at 1.6sec, as shown in Figure 9.

- A solar irradiation drop from 1000W/m² to 800W/m² after 0.4sec of start of simulation, then returns to 1000W/m² at 0.3 s as shown in Figure 10.
### Table 4. Characteristics Of Controlled PV System

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Symbol</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>PV-array power</td>
<td>$P_p$</td>
<td>1847W</td>
</tr>
<tr>
<td>DC bus capacitor</td>
<td>$C$</td>
<td>100µF</td>
</tr>
<tr>
<td>Switching frequency</td>
<td>$F_s$</td>
<td>10kHz</td>
</tr>
<tr>
<td>AC source</td>
<td>$V_g$</td>
<td>110V</td>
</tr>
<tr>
<td>Line frequency</td>
<td>$f$</td>
<td>50Hz</td>
</tr>
<tr>
<td>Filter parameters</td>
<td>$L$</td>
<td>12.5mH</td>
</tr>
<tr>
<td>$R$</td>
<td></td>
<td>0.5655 Ω</td>
</tr>
<tr>
<td>controller parameters</td>
<td>$c_1$</td>
<td>$8 \times 10^4$</td>
</tr>
<tr>
<td></td>
<td>$c_2$</td>
<td>$9.7 \times 10^4$</td>
</tr>
</tbody>
</table>

Figure 8. Simulation schema for the proposed PV system

Figure 9. Temperature changes

Figure 10. Solar irradiation changes

The first and second controllers are based respectively on (11) and (14), and use the same backstepping parameters (Table 4). Simulation results of the PV array power and voltage under transient condition are shown in Figure 11, which correspond very well to the MPP coordinates summarized in Table 2.
Figure 13 illustrates the change of direct and quadrature current components. It can be clearly seen that the second controller can track the reference values with a fast transient response, but the first controller is the most accurate and the least disruptive of the grid.

Figure 11. PV power and DC-bus voltage behaviors

Figure 12. Zoomed portion of figure 11

Figure 13. Current components behavior

Figure 14. shows the grid voltage and the injected current obtained with each one of the proposed controllers (the grid current scale was multiplied by 10).
It can also be observed that the amplitude of the phase current changes when the solar radiation or the temperature are varied. It can easily be seen in the zoomed portions (Figure 15) that the grid current is sinusoidal and in phase with the grid voltage which proving that the power factor unit is well achieved.

**Remark:** It should be noted that it is very difficult to tune backstepping parameters of the second controller to establish the stability, unlike the first controller whose parameters influence precisely on the precision and settling time.

Although the current of the first controller has fewer ripples compared to the second, the use of a second-order filter (LCL for example) will surely improve the quality of the injection.
5. CONCLUSION

In this paper, two Backstepping controllers have been developed for a three phase single stage grid connected photovoltaic system, without using the conventional DC/DC converter for MPPT control, in order to ensure the operation of the PV system at maximum power point with unity power factor. Using both theoretical analysis and simulation, it has been proven that the proposed controllers, although they require more computation, have given accurate results with virtually zero errors, it has also been deduced that the correct selection of system outputs helps to facilitate control tasks. Future work will deal with the mitigation of switching noise using LCL filter.

REFERENCES


BIOGRAPHIES OF AUTHORS

Mohammed El Malah was born in Morocco on November 02, 1980. He received the Master in Automatic, Signal Processing and Industrial Computing from Science and Technical Faculty, Hassan 1st University, Settat, Morocco in 2015. His research consists in the control of the linear and nonlinear systems with use of the advanced controller. Currently, he is preparing his PhD titled “Nonlinear control of renewable energy generation systems” in the Laboratory of System Analysis and Information Processing at Hassan 1st University.
Abdellfattah Ba-razzouk received the Master’s degree (M.Sc.A.) in industrial electronics from the Université du Québec à Trois-Rivières (UQTR), Quebec, Canada, in 1993, and the Ph.D. degree in electrical and computer engineering from the École Polytechnique de Montréal, Quebec, Canada, in 1998. From 1997 to 2003, he was a Lecturer in “motors modelling and control” at the Department of Electrical and Computer Engineering, UQTR. In September 1998, he joined the Hydro-Quebec Industrial Research Chair on Power and Electrical Energy, UQTR, where he has been a Professional Research Scientist working on “System Analysis and Information Processing Laboratory”, both at the Faculté des Sciences et Techniques, Université Hassan 1er of Settat, Morocco. His research interests include high performance control of adjustable speed drives, parameter identification and adaptive control of electrical motors, neural networks, real-time embedded control systems, renewable energy systems, modelling and computer aided design, and real-time simulation of power electronics systems using multiprocessors platforms.

M’hammed Guisser received the PhD in engineering science “Automatic and Industrial Computing” in 2009 from the “Higher National School of Electricity and Mechanics (ENSEM)”, University Hassan II, Casablanca, Morocco. His research interests include nonlinear control and state observer theory, robust and adaptive control, digital controller/observer and signal processing. He is involved in applications of these techniques to the control of unmanned aerial vehicles UAV, robotic systems and control of renewable energy. Currently, he is Assistant Professor in the Electrical Engineering Department of the “Centre Régional des Métiers de l’Éducation et de la Formation” (CRMEF), Settat, Morocco, and researcher in Laboratory ASTI, FST, Settat, University Hassan I Morocco.

Elhassane Abdelmounim received his PhD in applied Spectral analysis from Limoges University at science and technical Faculty, France in 1994. In 1996, he joined, as Professor, the applied physics department of the science and technical faculty of Hassan 1st University, Settat, Morocco. His current research interests include digital signal processing and machine learning. He is currently coordinator of a Bachelor of Science in electrical engineering and researcher in “ASTI” System Analysis and Information Technology Laboratory at science and technical faculty, Hassan 1st University, Settat, Morocco.

Mhamed Madark was born in Settat, Morocco, in 1987. He is a Ph.D. student. He received his B.Sc. degree in mathematics engineering from the Science and Technical Faculty of Hassan 1st University, Settat, Morocco, in 2013, the M.Sc. degree in Automatic, Signal Processing and Industrial Computing from the Science and Technical Faculty of Hassan 1st University, Settat, Morocco, in 2015. His research interests include the adaptive robust nonlinear control of the induction machine and robust nonlinear controller design for three phase grid connected PV systems.